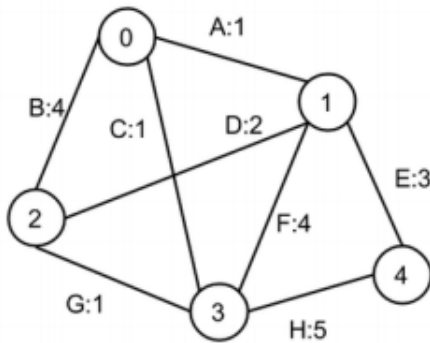


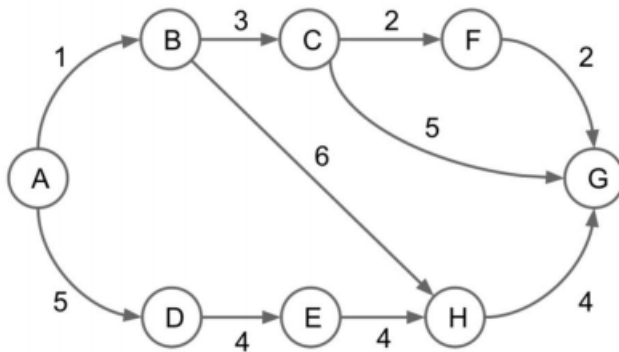
1 Warmup with MST and SP

- (a) For the graph below, use Kruskals algorithm to find the MST. The number on each edge is the weight, and the letter is a unique label you should use in your answer to specify that edge. **Provide the edges in the order theyd be inserted into the MST by Kruskals algorithm.** Break any ties using the alphabetical label. Use the blanks below. You may not need all blanks. **Give your answer in terms of the alphabetical labels**, e.g. if Kruskals starts with the edge between vertices 3 and 4, you would write H in the first blank.



- (b) Repeat part a, but using Prims algorithm, starting from vertex #3. **As before, give your answer in the order added to the MST and in terms of the alphabetical labels.** You may not need all of the blanks.

- (c) For the graph below, give the order in which Dijkstras Algorithm would visit each vertex, starting from vertex A.



- (g) Why are disjoint sets used in Kruskal's algorithm?
- (h) (T/F) The last edge added to the MST by Prim's algorithm is always the highest weight edge of the MST.

3 Shortest Path Algorithm Design

Design an efficient algorithm for the following problem: Given a weighted, undirected, and connected graph G where the weights of every edge in G are all integers between 1 and 10, and a starting vertex s in G , find the distance from s to every other vertex in the graph (where the distance between two vertices is defined as the weight of the shortest path connecting them).

Your algorithm must run asymptotically faster than Dijkstra's.

Hint: What other shortest path algorithms have we learned? Could we possibly modify the graph to apply other SP algorithms?